

MA 2121 - DIFFERENTIAL EQUATIONS OBJECTIVES

The general purpose of this course is to provide an understanding of ordinary differential equations (ODE's), and to give methods for solving them. Because differential equations express relationships between changing quantities, this material is applicable to many fields, and is essential for students of engineering or physical sciences.

Upon completion of this course, the student should be able to satisfy the following objectives.

A. GENERAL

1. Classify a differential equation in terms of ordinary/partial, order, linearity.
2. Verify a solution by substitution into the equation.
3. Explain the difference between the general solution to a differential equation and the unique solution to an initial value problem (IVP).
4. Determine whether a first- or second-order linear IVP has a unique solution over a given interval.
5. Apply initial conditions to a general solution to find the unique solution.

B. FIRST-ORDER EQUATIONS

1. Recognize a linear ODE and solve by an integrating factor.
2. Recognize a separable ODE and solve by separating variables.
3. Recognize an exact equation by checking partial derivatives, and solve by partial integration.
4. Solve appropriate applied problems involving exponential growth/decay or elementary mechanics.

C. SECOND-ORDER LINEAR EQUATIONS

1. Explain the principle of superposition. For a nonhomogeneous IVP, explain the relationships between the homogeneous (complementary) solution, a particular solution, the general solution, and the unique solution.
2. For solutions to a homogeneous equation: Define linear independence. Define the Wronskian, and use it to determine whether two solutions are linearly independent. Define the concept of a fundamental set of solutions, and how it relates to the general solution.
3. Given one solution to a homogeneous ODE, use reduction of order to find another solution.
4. Find the general solution to a homogeneous ODE with constant coefficients (whether the roots of the characteristic equation are distinct, repeated, or complex).
5. Explain when the method of undetermined coefficients is appropriate for finding a particular solution to a nonhomogeneous ODE. Apply this method.

6. Apply variation of parameters to find a particular solution.
7. Solve appropriate applied problems for mechanical or electronic oscillations. Explain the terms: free oscillations, forcing, damping, resonance, transient and steady response.
8. Find the general solution to a simple linear HIGHER-ORDER ODE with constant coefficients.

D. SERIES SOLUTIONS

1. Given a second-order ODE, determine whether a given point is an ordinary point, a regular singular point, or an irregular singular point.
2. For an ordinary point, find the first several terms in each of two linearly independent series solutions. Determine the minimum radius of convergence of these series from the coefficients of the ODE.
3. Recognize an Euler ODE and find the general solution.

E. LAPLACE TRANSFORMS

1. State the definition of the Laplace Transform, and use the definition to calculate the transform of a simple function. Given a function, determine whether the transform exists.
2. Use tables and general properties (linearity, derivative, translation) of Laplace Transforms to find the transform of a given function, or to find the inverse transform.
3. Use Laplace Transforms to solve a nonhomogeneous second-order IVP, where the forcing function could be discontinuous (express it in terms of unit step functions), or periodic, or involve impulse functions.
4. Define the convolution of two functions, and calculate it, given two functions. Use the convolution theorem to find the inverse transform of the product of two known transforms.

F. SYSTEMS OF EQUATIONS

1. Write a system of first-order linear ODE's in matrix form.
2. Find the general solution to a system of homogeneous first-order ODE's with constant coefficients (whether the eigenvalues are distinct, repeated, or complex).
3. Use variation of parameters to find a particular solution to a nonhomogeneous first-order system with constant coefficients. Find the general solution.
4. In relation to systems of ODE's, explain the terms: solution vector, linear independence, eigenvalues/eigenvectors, fundamental matrix.